

1. Chicken McNuggets originally came in boxes of 6, 9, or 20 McNuggets. A McNugget number is a positive integer that can be obtained by adding together orders of Chicken McNuggets, prior to consuming any.

(a) Prove that the following are McNugget numbers:

15, 35, 41, 42, 44, 45, 46, 47, 48, 49

(b) Prove that 43 is not a McNugget number

*Hint: Notice that 43 is odd*

(c) Prove that every integer  $n \geq 44$  is a McNugget number

*Hint: Strong Induction*

2. Write each of the following in set-builder notation:

(a) The set of integers that are multiples of 3

(b) The set of rational numbers whose square is less than 2

3. Let  $A = \{n \in \mathbb{Z} \mid n = 2k \text{ for some } k \in \mathbb{Z}\}$  and

$B = \{m \in \mathbb{Z} \mid m = 4j \text{ for some } j \in \mathbb{Z}\}$ .

Prove  $B \subseteq A$ . Is  $B \subset A$ ?

4. Let  $A = \{a, b, c\}$  and  $B = \{a, c, d, e\}$  with universal set  $U = \{a, b, c, d, e, f\}$ .

Find each of the following:

(a)  $A \cup B$

(d)  $B - A$

(g)  $A^c \cup B^c$

(b)  $A \cap B$

(e)  $A^c$

(h)  $(A \cap B)^c$

(c)  $A - B$

(f)  $A \times B$

(i)  $P(A)$