

# Work on these with your partner(s) at the board

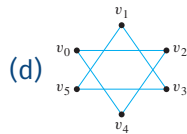
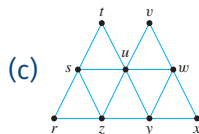
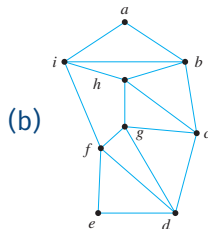
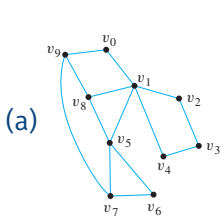
1. In the Petersen graph, find

- (a) a trail of length 5    (b) a path of length 9    (c) circuits of length 5, 6, 8, and 9

*Note: "length" means the number of edges*

2. Prove that if  $G$  has an Euler circuit, then every vertex of  $G$  has even degree.

3. For each graph, find an Euler circuit or explain why one does not exist.



Epp, Section 10.2

4. For each graph in #3, find an Hamiltonian circuit or explain why one does not exist.
5. For each graph, find an Hamiltonian circuit or explain why one does not exist.

