PROBLEM SET #6

Due Friday, March 22, 2024 @ 12:30 pm Submit as single pdf file to Canvas

Remember to review the Guidelines for WeBWorK and Problem Sets on the course webpage when writing up your solutions. The rule of thumb is that you should give enough explanation so that you could hand your assignment to a student who took Calc II last semester and they could follow your solutions.

1. Consider the series
$$\sum_{k=0}^{\infty} \frac{(-1)^k}{2k+1}$$

- (a) Show that the series converges.
- (b) Use WolframAlpha to compute S₅₀.How close is your partial sum to the exact value of the series? Why?
- 2. Consider the power series $P(x) = \sum_{k=0}^{\infty} (4x)^k$

What is the domain of P(x)? That is, for which values of x does P(x) converge?

3. Consider the power series $P(x) = \sum_{k=0}^{\infty} \left(\frac{x-5}{2}\right)^k$

What is the domain of P(x)? That is, for which values of x does P(x) converge?

4. Use the Maclaurin series for sin(x) and a four-function calculator $(+, -, \times, \div)$ to approximate sin(1) accurate with 0.001 of its exact value.

Explain how you know your answer is within this level of accuracy.