Explain why each integral is improper, determine if the integral converges or diverges, and for those that do converge, find the value of the integral.

$$1. \int_1^\infty \frac{1}{x^3} dx$$

5.
$$\int_0^1 \frac{1}{x^3} dx$$

$$2. \int_{1}^{\infty} \frac{1}{x} dx$$

6.
$$\int_0^1 \frac{1}{\sqrt{X}} dx$$

3.
$$\int_{1}^{\infty} \frac{1}{\sqrt{X}} dx$$

7.
$$\int_0^1 \frac{1}{x} dx$$

4.
$$\int_{1}^{\infty} \frac{1}{x^2 + 1} dx$$

8.
$$\int_{0}^{\pi/2} \tan(x) \, dx$$