

1. Use the Desmos to plot each of the following parametric curves. Observe how the curve is traced out.

What is the period of each curve? i.e. When does  $r(t)$  start “repeating”?

(a)  $r(t) = \langle \cos(t), -\sin(t) \rangle$

(b)  $r(t) = \langle \cos(t), \sin(2t) \rangle$

(c)  $r(t) = \langle \cos(t) \sin(2t), \sin(t) \sin(2t) \rangle$

(d)  $r(t) = \langle \cos(t) \sin(3t), \sin(t) \sin(t) \rangle$

(e)  $r(t) = \langle \cos(t) \sin(3t), \sin(t) \sin(3t) \rangle$

(f) Try other integer values for  $k$  in  $r(t) = \langle \cos(t) \sin(kt), \sin(t) \sin(kt) \rangle$

2. Let  $r(t) = \langle \cos(t), \sin(2t) \rangle$

(a) Sketch the graph of  $r(t)$  (Note this is the same function from 1(b))

(b) Find  $r'(t)$

(c) On your sketch, label the point  $r(0)$  and sketch the vector  $r'(0)$   
Use  $r(0)$  as the base point for  $r'(0)$

(d) Repeat (c) using  $r(t)$  and  $r'(t)$  for  $t = \frac{\pi}{6}, \frac{\pi}{4}, \frac{3\pi}{2}, \frac{5\pi}{2}$

(e) Use the Desmos file linked from the course webpage to verify your work

3. Use the Desmos file to explore the parametric curve

$$r(t) = \langle \cos(2t), \sin(t), \sin(t)^2 - \cos(3t) \rangle$$