

1. (a) Find the best fit line  $y = mx + b$  for the data points

x	1	1.5	2	3	3.1	3.2	4
y	8	9	15	10	18	23	19

- (b) Use the site <https://www.socscistatistics.com/tests/regression/> to find the least squares regression line for this data. Compare your answer to part (a).

2. Let  $A = \begin{bmatrix} 1 & -18 \\ -3 & 4 \end{bmatrix}$ ,  $\vec{v}_1 = \begin{bmatrix} -2 \\ 1 \end{bmatrix}$ ,  $\vec{v}_2 = \begin{bmatrix} 3 \\ 1 \end{bmatrix}$ ,  $\lambda_1 = 10$ ,  $\lambda_2 = -5$

- (a) Show that  $A$  has eigenvalues  $\lambda_1, \lambda_2$  with corresponding eigenvectors  $\vec{v}_1, \vec{v}_2$
- (b) Let  $P = [\vec{v}_1 \ \vec{v}_2]$ , the  $2 \times 2$  matrix with columns  $\vec{v}_1$  and  $\vec{v}_2$ . Compute  $AP$
- (c) Let  $D$  be the  $2 \times 2$  diagonal matrix with  $\lambda_1$  and  $\lambda_2$  on the diagonal. Compute  $PD$
- (d) Compute  $PDP^{-1}$ . Ponder