PROBLEM SET #7

Due Friday, November 8, 2024 @ 12:30 pm Submit as single pdf file to Canvas

Remember that you need to explain and show the steps in your answers!

1. Let $f(x) = \sin(x)$.

- (a) What is $P_3(x)$, the 3rd degree Maclaurin polynomial for $\sin(x)$?
- (b) Use your expression for $P_3(x)$ to approximate sin(3). Do you think your approximation is very accurate?
- (c) Find $P_9(x)$ and use it to approximate $\sin(3)$.
- (d) Compare your answer to (c) with the value that your calculator (or WolframAlpha) gives for sin(3). How close is your approximation?
- 2. (a) Use a 7th degree Maclaurin polynomial for $f(x) = e^x$ to approximate \sqrt{e} .
 - (b) Compare your answer to the value your calculator (or WolframAlpha) gives for \sqrt{e} . How close is your answer from part (a)?
- 3. Evaluate the following indefinite integrals.

(a)
$$\int x^4 - \sec(x) \tan(x) + \sin(x) dx$$

(b)
$$\int 3(\sin(x))^2 \cos(x) dx$$

(c)
$$\int 2^x - \frac{2}{x^3} dx$$