

Let  $f(x) = x^3 - x^2 - 2x$ ,  $g(x) = x + 3$ , and  $k(x) = 3x$

1. Let  $h(x) = k( f(x) )$ 
  - (a) Give the formula for  $h(x)$
  - (b) Plot  $y = h(x)$  and  $y = f(x)$  on the same set of axes
  - (c) How is the graph of  $y = h(x)$  related to the graph of  $y = f(x)$ ?
2.
  - (i) Repeat #1 for  $h(x) = f( k(x) )$
  - (ii) Repeat #1 for  $h(x) = g( f(x) )$
  - (iii) Repeat #1 for  $h(x) = f( g(x) )$
3. Explain how the graphs are related to the graph of  $y = f(x)$ 
  - (a)  $y = f(x) + a$
  - (b)  $y = f(x + a)$
  - (c)  $y = a f(x)$
  - (d)  $y = f(a x)$

**Remember**  $f(x) = x^3 - x^2 - 2x$ ,  $g(x) = x + 3$ , and  $k(x) = 3x$

4. Use the plot of  $y = f(x)$  to answer these questions
  - (a) What are the roots of  $f$ ? (i.e., For which  $x$ -values is  $f(x) = 0$ ?)
  - (b) For which  $x$ -values is  $f$  increasing? decreasing?
  - (c) What are the  $x$ -values where  $f$  has local maxes? mins?
  - (d) What are the  $x$ -values where  $f$  is concave up? concave down?
  
5. Repeat #4 for  $h(x) = k(f(x))$
  
6. Repeat #4 for  $h(x) = g(f(x))$
  
7. Repeat #4 for  $h(x) = f(g(x))$
  
8. Repeat #4 for  $h(x) = f(k(x))$