Work on these with your partner(s) at the board

- 1. Define a sequence by $a_1 = 1, a_2 = 3$, and $a_n = 3a_{n-1} 2a_{n-2} \ \forall n \in \mathbb{N}, n \ge 3$
 - (a) Compute the first six terms of the sequence, i.e, a_1, \ldots, a_6
 - (b) Form a conjecture for the value of a_n that depends only on n
 - (c) Use strong induction to prove your conjecture

Ernst, Exercise 4.27

2. Define the Fibonacci sequence by $f_1 = 1, f_2 = 1$, and $f_n = f_{n-1} + f_{n-2} \forall n \in \mathbb{N}, n \ge 3$ (a) Compute the first six terms of the sequence, i.e. f_1, \ldots, f_6

(b) Use strong induction to prove that $\left(\frac{3}{2}\right)^{n-2} \leq f_n \leq 2^n \quad \forall n \in \mathbb{N}$