## Work on these with your partner(s) at the board

1. Define a sequence by $a_{1}=1, a_{2}=3$, and $a_{n}=3 a_{n-1}-2 a_{n-2} \forall n \in \mathbb{N}, n \geq 3$
(a) Compute the first six terms of the sequence, i.e, $a_{1}, \ldots, a_{6}$
(b) Form a conjecture for the value of $a_{n}$ that depends only on $n$
(c) Use strong induction to prove your conjecture

Ernst, Exercise 4.27
2. Define the Fibonacci sequence by $f_{1}=1, f_{2}=1$, and $f_{n}=f_{n-1}+f_{n-2} \forall n \in \mathbb{N}, n \geq 3$
(a) Compute the first six terms of the sequence, i.e, $f_{1}, \ldots, f_{6}$
(b) Use strong induction to prove that $\left(\frac{3}{2}\right)^{n-2} \leq f_{n} \leq 2^{n} \quad \forall n \in \mathbb{N}$ Ernst, Exercise 4.29

