

Let  $\vec{u}_1 = \begin{bmatrix} -1 \\ -3 \\ -2 \end{bmatrix}$ ,  $\vec{u}_2 = \begin{bmatrix} -2 \\ 0 \\ 1 \end{bmatrix}$ ,  $\vec{u}_3 = \begin{bmatrix} 3 \\ -5 \\ 6 \end{bmatrix}$ , and  $\vec{y} = \begin{bmatrix} 9 \\ -8 \\ 4 \end{bmatrix}$

1. Verify that  $\mathcal{B} = \{\vec{u}_1, \vec{u}_2, \vec{u}_3\}$  is an orthogonal basis for  $\mathbb{R}^3$
2. Find  $\hat{y}_1$ , the orthogonal projection of  $\vec{y}$  onto  $\vec{u}_1$   
 $\hat{y}_2$ , the orthogonal projection of  $\vec{y}$  onto  $\vec{u}_2$   
 $\hat{y}_3$ , the orthogonal projection of  $\vec{y}$  onto  $\vec{u}_3$
3. Write  $\vec{y}$  as a linear combination of  $\vec{u}_1, \vec{u}_2, \vec{u}_3$
4. Form the matrix  $A = \begin{bmatrix} \vec{u}_1 & \vec{u}_2 & \vec{u}_3 \end{bmatrix}$ , and calculate  $A^T A$