## Problem Set \#1

Due Thursday, February 3, 2022 @ midnight EDT

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Remember that you need to explain and show the steps in your answers!

1. Let $f(x)=x^{3}-5 x, g(x)=x-4$, and $h(x)=x+2$.
(a) Evaluate $(f \circ g \circ h)(-3)$
(b) How is the graph of $y=(f \circ g)(x)$ related to the graph of $y=f(x)$ ?
(c) How is the graph of $y=(h \circ f)(x)$ related to the graph of $y=f(x)$ ?
2. The graph of $y=f(x)$ is shown below.
(a) Is $f(-2)$ positive, negative or zero? Explain.
(b) Is $f^{\prime}(-2)$ positive, negative or zero? Explain.
(c) Give a value $x=a$ where $f(a)<0$ and $f^{\prime}(a)>0$. Explain.

3. Use the graph of $y=f(x)$ from Problem 2.
(a) Copy the graph of $y=f(x)$ and sketch a graph of $y=f^{\prime}(x)$ on the same set of axes.
(b) Is $f^{\prime \prime}(-3)$ positive, negative, or zero? Why?
4. Solve the equation $\ln \left(x^{2}+4\right)=2$ for $x$. Be sure to show your steps.
