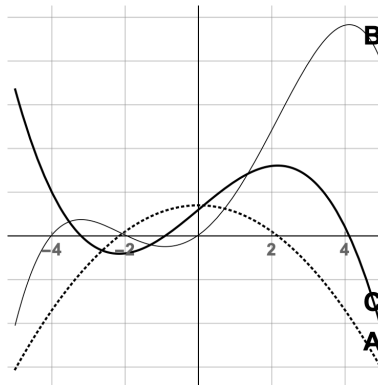
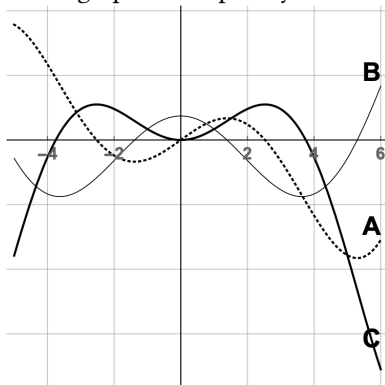


1. The graphs of  $f$ ,  $f'$ , and  $f''$  are shown below on the same set of axes.

Label each on the graph and explain your answers.



2. Suppose that the graph labeled C on the left graph in #1 is the graph of  $g'(x)$ .
- Is  $g$  concave up or concave down at  $x = -1$ ?
  - Find all critical points of  $g$  and label them as local maxima, local minima, or neither.
  - Suppose  $g(-2) = 5$ . Could  $g(1) = 0$ ? Could  $g(1) = 10$ ?
3. Suppose that the graph labeled B on the right graph in #1 is the graph of  $h''(x)$ .
- What are the inflection points of  $h$ ?
  - If the critical points of  $h$  are  $x = -3$ ,  $x = -1$ , and  $x = 2$ , use the Second Derivative Test to classify each as a local maxima or local minima, if possible.
4. Evaluate the following limits. Be sure to explain your answers.

$$(a) \lim_{x \rightarrow \infty} x^2 e^{-3x} \quad (b) \lim_{x \rightarrow \infty} \frac{\ln(x)}{\cos(3x) + 5}$$

5. Let  $f(x) = 3x^5 - 25x^3 + 7$
- Find all critical points of  $f$  and classify them as local maxima, local minima, or neither.
  - On which intervals is  $f$  increasing? Decreasing?
  - Find the inflection points of  $f$ .
  - On which intervals is  $f$  concave up? Concave down?
  - Use this information to sketch a graph of  $y = f(x)$ .
6. Verify that  $F(x) = e^x x - e^x + 3$  is an antiderivative of  $f(x) = xe^x$ .  
What important fact does the Mean Value Theorem tell us about any other antiderivative of  $f$ ?
7. Why do we use radians to measure angles in calculus rather than degrees?
8. Let  $f(x) = e^x$ .
- Find the equation of the line tangent to  $y = f(x)$  at  $x = 0$ . Use this to approximate  $e$ .
  - What is the fifth degree Maclaurin polynomial of  $f(x)$ ? Use it to approximate  $e$ .
  - Which approximation do you think will be more accurate? Why?
9. Let  $g(x) = \sin(x^3)$ . What is  $g^{(5)}(0)$ ?  $g^{(9)}(0)$ ?  $g^{(100)}(0)$ ?  $g^{(123)}(0)$ ?  
Be sure to justify your answers.