- 1. Let p = 11
 - (a) What are the possible orders for elements in \mathbb{Z}_p^* ?
 - (b) Find a generator a of \mathbb{Z}_p^* .
 - (c) Fill in the following table:

k	a ^k	mod p	$ord(a^k)$
1			
2			
:			
p-1			

- (d) For which values of k is a^k a generator?
- (e) How are the values in your last answer related to $\phi(p-1)$?
- (f) How many generators does \mathbb{Z}_p^* have?
- (g) What is a desirable order of α for DHKE using modulus p? What is a desirable value of α for DHKE using modulus p?

- Repeat the previous problem with p = 23.
 Note that your table will have 22 rows.
 The Mathematica command MultiplicativeOrder[] might be handy.
- Show that p = 1786 511 is a poor choice as the modulus for DHKE.
 The Mathematica commands PrimeQ[] and FactorInteger[] may be useful.
- 4. Show that $p=1786\,553$ is a reasonable choice for DHKE and find an appropriate value α .
- 5. Go to https://www.rfc-editor.org/rfc/rfc3526 and verify that the given values for the 2048-bit prime and α are reasonable choices for DHKE.
 - Note that when this page says "The generator is: 2", it does *not* mean that 2 is a generator of \mathbb{Z}_p^* , but rather that $\alpha=2$ is a good choice for Diffie-Hellman.