

The purpose of these problems is to get some insight into picking the parameters p and α for DHKE

1. Let $p = 7$

- (a) Let $\alpha = 2$ and calculate $\alpha^i \pmod p$ for $i = 1, 2, \dots, 6$
How many unique values do you get?

Remember the *Mathematica* command `Table[Mod[2^i,7], {i,1,6}]`
FYI, this also works in WolframAlpha

(b) Repeat (a) for $\alpha = 3$

(c) Based on your answers, using $p = 7$, would you choose $\alpha = 2$ or $\alpha = 3$ for DHKE? Explain.

2. Let $p = 31$ and repeat #1 with $i = 1, \dots, 30$ for $\alpha = 2$ and $\alpha = 3$

3. What are the elements of \mathbb{Z}_{12}^* ? of \mathbb{Z}_{11}^* ?
4. What is $\text{ord}(2)$ in \mathbb{Z}_{31}^* ? $\text{ord}(3)$ in \mathbb{Z}_{31}^* ? $\text{ord}(7)$ in \mathbb{Z}_{31}^* ?
5. Is 2 a generator in \mathbb{Z}_{31}^* ? How about 3? How about 7?
6. What connection do you see to DHKE?