

Let  $L \subset \mathbb{R}^3$  be a lattice with bases  $\mathcal{B}_1 = \{\vec{v}_1, \vec{v}_2, \vec{v}_3\}$  and  $\mathcal{B}_2 = \{\vec{w}_1, \vec{w}_2, \vec{w}_3\}$  where

$$\vec{v}_1 = \langle 1, 3, 1 \rangle$$

$$\vec{v}_2 = \langle -2, 1, 1 \rangle$$

$$\vec{v}_3 = \langle 3, -2, -4 \rangle$$

$$\vec{w}_1 = \langle 18, -5, -5 \rangle$$

$$\vec{w}_2 = \langle -59, -24, 2 \rangle$$

$$\vec{w}_3 = \langle -27, -8, 2 \rangle$$

1. Verify that  $\mathcal{B}_1$  and  $\mathcal{B}_2$  are bases for the same lattice by placing  $\mathcal{B}_1$  in the rows of a matrix  $A$ ,  $\mathcal{B}_2$  in the rows of a matrix  $B$  and verify that there is a matrix  $U$  with determinant 1 such that  $UA = B$ .
2. Compute the Hadamard Ratio for  $\mathcal{B}_1$  and  $\mathcal{B}_2$ .
3. Use Babai's Algorithm to solve the CVP for  $\vec{w} = (13, -3, 7)$  using  $\mathcal{B}_1$ . Repeat using  $\mathcal{B}_2$ .
4. What is the value of  $\|\vec{v} - \vec{w}\|$  for your answers from 3?