

These are only a *few* sample problems to *help* you prepare for the exam. You should also be certain that you completely understand the WeBWorK assignments, Problems Sets, in-class work, and your class notes.

- Is it possible that the terms of a series converge but the partial sums diverge? Explain.
  - Can the partial sums converge but the terms diverge? Explain.
- Do the following series diverge, converge conditionally, or converge absolutely? Be sure to justify your answer by giving reference to the appropriate theorems and/or tests.

$$(a) \sum_{k=3}^{\infty} (-1)^{k+1} \frac{\sqrt{k+1}}{\ln(k)}$$

$$(c) \sum_{j=0}^{\infty} \cos(j) j^5 e^{-j^3}$$

$$(b) \sum_{k=3}^{\infty} \frac{2k}{4k^8 + 7k^2 + 6}$$

$$(d) \sum_{k=10}^{\infty} (-1)^k \frac{3}{4k+2}$$

Pick one of the series that converges. How close does  $S_{75}$  approximate the value of the series?

$$3. \text{ Let } \mathcal{I} = \int_0^1 \cos(x^2) dx.$$

- Calculate  $\mathcal{I}$  accurate within 0.001 by hand with the use of only a four function (+, -, ×, ÷) calculator.
  - Find a value of  $n$  such that  $T_n$  approximates  $\mathcal{I}$  accurate within 0.001.  
It may be useful to know that the absolute value of the second derivative of  $\cos(x^2)$  is less than 4 on the interval  $[0, 1]$ .
4. Find the *exact* value of the following by hand (no decimal approximations!)

$$(a) \sum_{k=42}^{\infty} \frac{1}{4^k}$$

$$(c) \sum_{k=0}^{\infty} \frac{1}{3^k k!}$$

$$(b) \sum_{k=0}^{326} \left(\frac{3}{7}\right)^k$$

$$(d) \sum_{k=0}^{\infty} (-1)^k \frac{(1/\sqrt{3})^{2k+1}}{2k+1}$$

5. Let  $a(x)$  be a continuous function that is positive and decreasing for all  $x \geq 1$ , and let  $a_k = a(k)$ .
- Rank the following values. Draw diagrams to explain your answer.

$$A = \sum_{k=5}^{\infty} a_k \quad B = \sum_{k=6}^{\infty} a_k \quad C = \int_5^{\infty} a(x) dx$$

- Explain how your answer is related to the Integral Test for series.