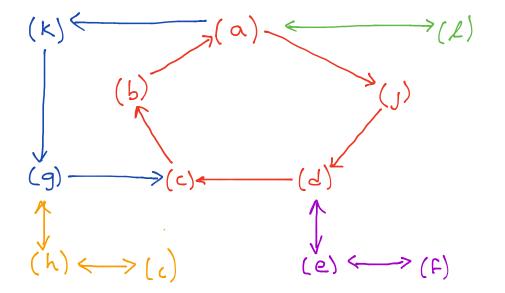
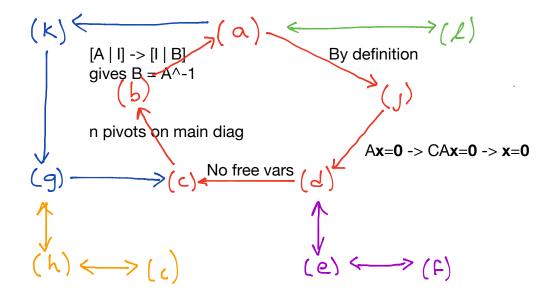
## **The Invertible Matrix Theorem**: Let A be a square $n \times n$ matrix. Then the following statements are equivalent.

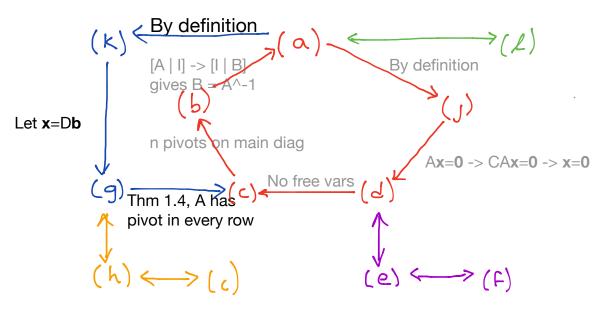
- a. A is an invertible matrix.
- b. A is row equivalent to the  $n \times n$  identity matrix.
- c. A has n pivot positions.
- d. The equation  $A\mathbf{x} = \mathbf{0}$  has only the trivial solution.
- e. The columns of A form a linearly independent set.
- f. The linear transformation  $\mathbf{x} \to A\mathbf{x}$  is one-to-one.
- g. The equation  $A\mathbf{x} = \mathbf{b}$ . has at least one solution for each  $\mathbf{b}$  in  $\mathbb{R}^n$ .
- h. The columns of A span  $\mathbb{R}^n$ .
- i. The linear transformation  $\mathbf{x} \to A\mathbf{x}$  maps  $\mathbb{R}^n$  onto  $\mathbb{R}^n$ .
- j. There is an  $n \times n$  matrix C such that CA = I.
- k. There is an  $n \times n$  matrix D such that AD = I.
- I.  $A^T$  is an invertible matrix.

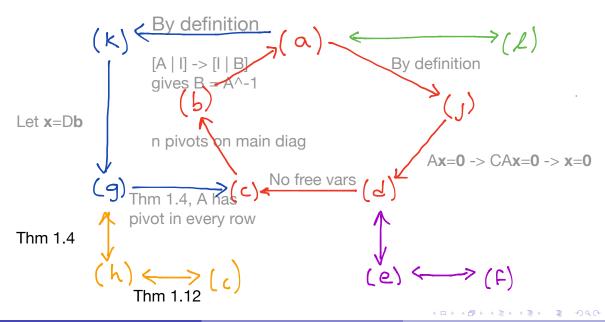


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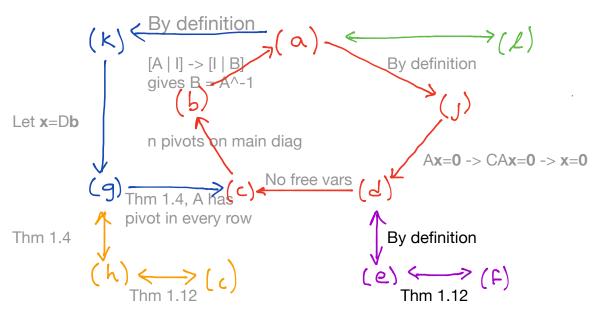


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