

$$\text{Let } \mathbf{u}_1 = \begin{bmatrix} -1 \\ -3 \\ -2 \end{bmatrix}, \mathbf{u}_2 = \begin{bmatrix} -2 \\ 0 \\ 1 \end{bmatrix}, \mathbf{u}_3 = \begin{bmatrix} 3 \\ -5 \\ 6 \end{bmatrix}, \text{ and } \mathbf{y} = \begin{bmatrix} 9 \\ -8 \\ 4 \end{bmatrix}.$$

1. Verify that $\{\mathbf{u}_1, \mathbf{u}_2, \mathbf{u}_3\}$ is an orthogonal basis for \mathbb{R}^3 .
2. Find $\hat{\mathbf{y}}_1$, the orthogonal projection of \mathbf{y} onto \mathbf{u}_1
 $\hat{\mathbf{y}}_2$, the orthogonal projection of \mathbf{y} onto \mathbf{u}_2 .
 $\hat{\mathbf{y}}_3$, the orthogonal projection of \mathbf{y} onto \mathbf{u}_3 .
3. Find scalars c_1 , c_2 , and c_3 such that $\mathbf{y} = c_1\mathbf{u}_1 + c_2\mathbf{u}_2 + c_3\mathbf{u}_3$
4. Form the matrix $A = [\mathbf{u}_1 \quad \mathbf{u}_2 \quad \mathbf{u}_3]$, and calculate $A^T A$.