Math 217 Voting Theory 1

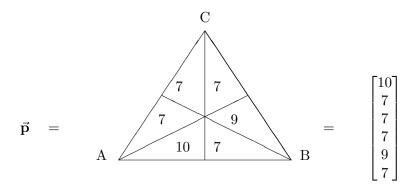
Place fundamental vectors  $K, R_1, R_2, C_y, B_1, B_2$  in columns of matrix M.

$$M = \begin{bmatrix} 1 & 1 & 0 & 1 & 2 & 1 \\ 1 & 0 & 1 & 0 & 2 & 0 \\ 1 & 0 & 0 & 1 & 1 & 0 \\ 1 & 1 & 0 & 0 & 0 & 1 \\ 1 & 0 & 1 & 1 & 0 & 2 \\ 1 & 0 & 0 & 0 & 1 & 2 \end{bmatrix}$$

$$M^{-1} = \frac{1}{6} \begin{bmatrix} -4 & 1 & 5 & 4 & -1 & 1 \\ 3 & 0 & -3 & 3 & 0 & -3 \\ 0 & 3 & -3 & 0 & 3 & -3 \\ 2 & -2 & 2 & -2 & 2 & -2 \\ 2 & 1 & -1 & -2 & -1 & 1 \\ 1 & -1 & -2 & -1 & 1 & 2 \end{bmatrix}$$

If  $\vec{\mathbf{p}}$  is a profile in the standard coordinates, then  $M^{-1}\vec{\mathbf{p}}$  gives the decomposition in terms of the fundamental vectors.

For example, if



Then the decomposition in terms of the fundamental vectors is

$$M^{-1}\vec{\mathbf{p}} = \frac{1}{6} \begin{bmatrix} -4 & 1 & 5 & 4 & -1 & 1 \\ 3 & 0 & -3 & 3 & 0 & -3 \\ 0 & 3 & -3 & 0 & 3 & -3 \\ 2 & -2 & 2 & -2 & 2 & -2 \\ 2 & 1 & -1 & -2 & -1 & 1 \\ 1 & -1 & -2 & -1 & 1 & 2 \end{bmatrix} \begin{bmatrix} 10 \\ 7 \\ 7 \\ 9 \\ 7 \end{bmatrix} = \frac{1}{6} \begin{bmatrix} 28 \\ 9 \\ 6 \\ 10 \\ 4 \\ 5 \end{bmatrix}$$
$$= \frac{1}{6} (28K + 9R_1 + 6R_2 + 10C_y + 4B_1 + 5B_2)$$

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