

A hurricane is traveling due north at a speed of 20 knots (nautical miles per hour). A boat with a maximum speed of 12 knots is located 10 nautical miles north and 5 nautical miles east of the hurricane.

1. If the boat takes a heading of due north, determine how close the hurricane will get to the boat and the time when this occurs.
Hint: No calculus required!
2. If the boat takes a heading of due east, determine how close the hurricane will get to the boat and the time when this occurs.
Hint: Calculus required!
3. If the boat takes a heading of northeast, determine how close the hurricane will get to the boat and the time when this occurs.
4. If the boat takes a heading of θ (measured as an angle from due east), determine how close the hurricane will get to the boat and the time when this occurs. These will both be functions of θ .
5. If the captain wants to maximize the minimum distance between the hurricane and the boat, what heading should he choose?