

1. Find the area of the region that is above the graph of  $y = 2x^2$  and below the graph of  $y = -5x + 3$ .

2. Recall that we cannot find an antiderivative for  $f(x) = \sin(x^2)$  to evaluate  $\mathcal{I} = \int_0^1 \sin(x^2) dx$ .

There are a couple of ways we can approximate  $\mathcal{I}$ .

(a) Plot  $y = f(x)$ , and calculate  $L_{10}$  and  $R_{10}$ .

Will  $L_{10}$  overestimate or underestimate  $\mathcal{I}$ ? How about  $R_{10}$ ?

How accurate is your approximation to the exact value of  $\mathcal{I}$ ?

(b) Find the Taylor Polynomial of degree 7 for  $\sin(x)$ .

(You can also check your notes from March 9).

Use this to find a Taylor polynomial for  $f(x)$ .

Substitute this Taylor polynomial into the integral and evaluate to approximate  $\mathcal{I}$ .