

1. Let $I = \int_1^{\infty} \frac{\pi}{x^3 + 2x + 7} dx$

a. Show that I converges

b. How closely does the definite integral $I_1 = \int_1^7 \frac{\pi}{x^3 + 2x + 7} dx$ approximate I ?

c. Find a definite integral that approximates I accurate with 0.005

2. Find the exact value of each integral.

a. $\int_{1/2}^{\infty} \frac{\arctan(2x)}{1 + 4x^2} dx$

b. $\int_1^{\infty} x^3 e^{-x^2} dx$