

1. For each series:

- (i) Find the limit of $\{a_k\}$, the sequence of terms of the series
- (ii) Show that the series converges
- (iii) Find the limit of $\{S_n\}$, the sequence of partial sums of the series

$$(a) \sum_{k=0}^{\infty} 7e^{-k} \quad (b) \sum_{k=13}^{\infty} \left(-\frac{3}{7}\right)^k$$

2. Do the following series converge or diverge?

$$(a) \sum_{k=1}^{\infty} \frac{1}{3^k + 2}$$

$$(b) \sum_{k=2}^{\infty} \frac{1}{k^2}$$

Hint: Draw a picture comparing with $\int_1^{\infty} \frac{1}{x^2} dx$.

$$(c) \sum_{k=1}^{\infty} \frac{1}{k}$$

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