

Let $\mathcal{I} = \int_{-\pi}^{\pi} e^{\sin(x)} dx$.

Approximate \mathcal{I} accurate within

1. 0.01 using a right sum
2. 0.001 using a trapezoid sum
3. 0.0001 using a midpoint sum

Let $\mathcal{I} = \int_0^2 e^{x^2} dx$

1. Plot the integrand to verify that it is monotone over the interval of integration.
2. Calculate L_{1500} and R_{1500} . How close are these to the actual value of \mathcal{I} ?
3. Use Theorem 3 to find a value for n such that $|\mathcal{I} - L_n|$ is guaranteed to be less than 0.10. How does this compare to #2? Explain.
4. Will M_{100} overestimate or underestimate \mathcal{I} ? How about T_{100} ?
5. Calculate M_{100} and T_{100} .
How close are these to the actual value of \mathcal{I} ?
6. What does Theorem 3 tell you about $|\mathcal{I} - M_{100}|$?
How does this compare to #5? Explain.