

1. Let $I = \int_1^{\infty} \frac{1}{x^5 + 3x} dx$

(a) Show that I converges.

(b) Find a definite integral I_1 that will approximate I within 0.002 of its true value.

(c) Approximate I_1 within 0.002 of its actual value.

(d) Explain how you have approximated I within 0.004 of its actual value.

2. Find the exact value of $\int_1^{\infty} e^{-x} x dx$.