

Let  $g(x, y) = x^2 - 4x + y^2 - 8y + xy + 20$ .

1. Find  $g_x(3, 4)$  and  $g_y(3, 4)$ .
2. On the same set of axes, plot  $g(x, y)$  and the paths on the surface corresponding to  $x = 3$  and  $y = 4$ . Do your answers from #1 agree with this?
3. Find the absolute minimum value of  $g(x, y)$ . Verify your answer using a contour plot.