Let 
$$f(x,y) = \frac{6x^3y}{2x^4 + y^4}$$
, and consider  $\lim_{(x,y)\to(0,0)} f(x,y)$ .

- 1. Find the limit as you approach the origin along the *x*-axis.
- 2. Find the limit as you approach the origin along the y-axis.
- 3. Find the limit as you approach the origin along the line y = x.
- 4. Find the limit as you approach the origin along the line y = mx.
- 5. Use a 3-D plot, a contour plot, and a density plot to explain the behavior of f near the origin.

T. Ratliff, Math 236 February 25, 2005 - p.1