Let $f(x, y)=\frac{6 x^{3} y}{2 x^{4}+y^{4}}$, and consider $\lim _{(x, y) \rightarrow(0,0)} f(x, y)$.

1. Find the limit as you approach the origin along the $x$-axis.
2. Find the limit as you approach the origin along the $y$-axis.
3. Find the limit as you approach the origin along the line $y=x$.
4. Find the limit as you approach the origin along the line $y=m x$.
5. Use a 3-D plot, a contour plot, and a density plot to explain the behavior of $f$ near the origin.
