Evaluate the following integrals using integration by parts, and check your answers!!

$$1. \int x \ln(x) \ dx$$

$$2. \int xe^x \ dx$$

$$3. \int x^3 e^{x^2} dx$$

$$4. \int \ln(x) \ dx$$

$$5. \int e^x \cos(x) \ dx$$

(Hint:
$$u = x^2$$
 and $dv = xe^{x^2}dx$)

(Hint:
$$u = \ln(x)$$
 and $dv = dx$)