Let $f(x)=\cos (x)$ and let $x_{0}=\frac{\pi}{2}$.

1. Find $P_{3}(x)$
2. Verify your answer by graphing $P_{3}(x)$ and $f(x)$ on the same set of axes with $-\pi \leq x \leq 2 \pi$
3. Use $P_{3}(2)$ to approximate $\cos (2)$
4. How accurate is your answer?
5. Find a value of $n$ so that $P_{n}(2)$ approximates $\cos (2)$ accurate within $10^{-10}$.
