Evaluate the following integrals using integration by parts, and *check your answers!!*

1.
$$\int x \ln(x) dx$$

2.
$$\int xe^{x} dx$$

3.
$$\int x^{3}e^{x^{2}} dx$$
 (Hint: $u = x^{2}$ and $dv = xe^{x^{2}} dx$)
4.
$$\int \ln(x) dx$$
 (Hint: $u = \ln(x)$ and $dv = dx$)
5.
$$\int e^{x} \cos(x) dx$$