

1. Determine if the following sets of vectors are linearly independent or linearly dependent.

$$(a) \quad \vec{v}_1 = \begin{bmatrix} 2 \\ 0 \\ 3 \end{bmatrix} \quad \vec{v}_2 = \begin{bmatrix} 0 \\ -1 \\ 6 \end{bmatrix} \quad \vec{v}_3 = \begin{bmatrix} -2 \\ -4 \\ 21 \end{bmatrix}$$

$$(b) \quad \text{The columns of } A = \begin{bmatrix} 1 & 2 & -3 \\ 2 & -3 & 4 \\ -1 & 3 & 2 \end{bmatrix}$$

2. If A is 4×5 , are the columns linearly independent or linearly dependent? What if A is 5×4 ?
3. If the system $A\vec{x} = \vec{b}$ has a unique solution, are the columns of A linearly independent or linearly dependent? Why?