

Let  $I = \int_0^1 e^{-x^2} dx$ .

Use Theorem 1 to answer the following.

1. How close will  $L_{5000}$  approximate  $I$ ?  $R_{5000}$ ?  $T_{5000}$ ?
2. Find a value of  $n$  so that  $L_n$  approximates  $I$  within 0.00001 of the actual value.
3. Repeat #2 but with  $T_n$ .

## Recap for Today

- Even if we can't find an antiderivative, we can approximate an integral. The goal is to determine how close the approximation is to the actual value of the integral.
- If the  $f(x)$  is monotone on  $[a, b]$ , we can determine how close  $L_n$ ,  $R_n$  and  $T_n$  are to  $\int_a^b f(x) dx$  *without knowing the exact value of the integral!*