

1. Evaluate the following integrals:

(a)  $\int x\sqrt{x-1}dx$  ( $u = x - 1$ )

(b)  $\int x \tan(x^2) dx$

(c)  $\int \frac{1}{\sqrt{x}(\sqrt{x}+2)^3} dx$

2. Find the area of each region specified.

(a) Between  $y = 2\sin(x)\cos(x) + x$  and the  $x$ -axis for  $0 \leq x \leq \pi$

(b) Between  $y = \frac{x}{2+x^2}$  and the  $x$ -axis for  $0 \leq x \leq 3$

(c) Between  $y = \frac{x}{2+x}$  and the  $x$ -axis for  $0 \leq x \leq 3$

(d) Bounded by  $y = x^3 - x$  and  $y = 3x$

3. Find the average value of each function on the specified interval

(a)  $f(x) = x \sin(x^2)$  on  $[0, \sqrt{\pi}]$

(b)  $f(x) = \cos(x)^4 \sin(x)$  on  $[0, \pi]$

4. Evaluate the following definite integrals.

If you cannot find an antiderivative, then estimate the value of the integral.

(a)  $\int_{-1}^1 \sin(x)e^{x^2} dx$  (Hint: Look at the graph)

(b)  $\int_{-1}^0 e^{x^2} dx$  (Hint: Think Taylor polynomials)