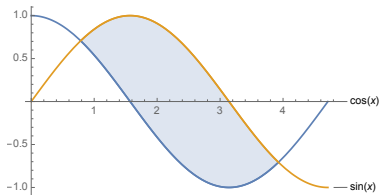


We cannot find an antiderivative for  $\sin(x^2)$ , but there are a couple of ways we can approach finding an approximation for

$$\mathcal{I} = \int_0^1 \sin(x^2) dx$$

1. Plot  $y = \sin(x^2)$ ,
  - (a) Calculate  $L_{10}$  and  $R_{10}$ .
  - (b) Will  $L_{10}$  overestimate or underestimate  $\mathcal{I}$ ? How about  $R_{10}$ ?
  - (c) How accurate is your approximation to the exact value of  $\mathcal{I}$ ?
2. Find the Taylor Polynomial of degree 7 for  $\sin(x)$  (Check your notes from March 29)
  - (a) Use this to find a Taylor polynomial for  $\sin(x^2)$ .
  - (b) Substitute this Taylor polynomial into the integral and evaluate to approximate  $\mathcal{I}$ .

1. Find the area of the region shaded in blue, bounded by the graphs of  $y = \sin(x)$  and  $y = \cos(x)$



2. Find the area of the region bounded by the graphs of  $y = x^3$  and  $y = x^2 + x$

