

Let

$$\begin{aligned} \mathbf{v}_1 &= (1, 3, 18, 2) \\ \mathbf{v}_2 &= (2, -1, 9, 0) \\ \mathbf{v}_3 &= (3, 2, -4, 1) \\ \mathbf{v}_4 &= (4, 7, 1, 3) \end{aligned} \quad \text{and} \quad A = \begin{bmatrix} 1 & 3 & 2 \\ -2 & 1 & 4 \\ 6 & 2 & 1 \\ 5 & -17 & 32 \end{bmatrix}$$

1. The vectors $\{\mathbf{v}_1, \mathbf{v}_2, \mathbf{v}_3, \mathbf{v}_4\}$ span \mathbb{R}^4
2. The columns of A span \mathbb{R}^4
3. The equation $B\mathbf{x} = \mathbf{b}$ has a unique solution where $B = [\mathbf{v}_1 \ \mathbf{v}_2 \ \mathbf{v}_3 \ \mathbf{v}_4]$ and $\mathbf{b} = (72, -128, \pi, e^{-411})$
4. There exists $\mathbf{b} \in \mathbb{R}^4$ such that $A\mathbf{x} = \mathbf{b}$ has infinitely many solutions.