1. Let
$$A = \begin{bmatrix} 1 & -18 \\ -3 & 4 \end{bmatrix}$$

- (a) Find the eigenvectors and eigenvalues of A
- (b) Factor A into a product PDP^{-1} .
- (c) Use your factorization to compute A^{20} .
- 2. Construct a matrix A with eigenvalues 0, 2, 3 and eigenvectors (1, 3, -2), (3, 2, 0), and (-2, 1, 4), respectively.

3. Is
$$A = \begin{bmatrix} 3 & -1 \\ 1 & 1 \end{bmatrix}$$
 diagonalizable?

- 4. True or False
 - (a) If A is diagonalizable, then A invertible.
 - (b) If A is invertible, then A is diagonalizable.