Let $\mathcal{I}=\int_{0}^{1} x \sin \left(x^{2}\right) d x$

1. Calculate $L_{4}$ by hand. Does this overestimate or underestimate $\mathcal{I}$ ?
2. Write $L_{10}$ using sigma notation.
3. Use Maple to draw and to calculate $L_{10}$ and $R_{10}$ (use the Tools - Tutors - Calculus Single Variable - Approximate Integration menu. )
4. How does $\mathcal{I}$ compare to $L_{10}$ and $R_{10}$ ?
5. Find a value of $n$ so that $L_{n}$ and $R_{n}$ approximate $\mathcal{I}$ accurate within 0.01 . How are you certain that your value of $n$ is correct?
