

$$\text{Let } \vec{\mathbf{u}}_1 = \begin{bmatrix} 1 \\ 2 \\ 3 \end{bmatrix}, \vec{\mathbf{u}}_2 = \begin{bmatrix} 3 \\ 0 \\ 1 \end{bmatrix}, \text{ and } \vec{\mathbf{u}}_3 = \begin{bmatrix} 1 \\ -1 \\ -1 \end{bmatrix}$$

1. Find a vector $\vec{\mathbf{x}}$ in \mathbb{R}^3 that is orthogonal to $\vec{\mathbf{u}}_1$.
2. Find a vector $\vec{\mathbf{y}}$ that is orthogonal to both $\vec{\mathbf{u}}_1$ and $\vec{\mathbf{u}}_2$.
3. Find all vectors $\vec{\mathbf{z}}$ in \mathbb{R}^3 that are orthogonal to $\vec{\mathbf{u}}_1$, $\vec{\mathbf{u}}_2$, and $\vec{\mathbf{u}}_3$.

4. Let $A = \begin{bmatrix} \vec{\mathbf{u}}_1 \\ \vec{\mathbf{u}}_2 \\ \vec{\mathbf{u}}_3 \end{bmatrix}$. How is each $\vec{\mathbf{z}}$ from part 3 related to $\text{row}(A)$?

Which fundamental subspace of A do the $\vec{\mathbf{z}}$ lie in?